

PART 1

$$\begin{aligned}
 1. \quad & 2(1+2+2^2+2^3+\dots+2^{n-1})=510 \\
 & 2(1+2+2^2+\dots+2^{n-2})=254 \\
 & 2+2^2+\dots+2^{n-2}=126 \\
 & 2+\dots+2^{n-3}=62 \\
 & 2+\dots+2^{n-4}=30 \\
 & 2+\dots+2^{n-5}=14 \\
 & 2+\dots+2^{n-6}=6 \\
 & 2+\dots+2^{n-7}=2 \\
 & \therefore n=7
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & a_1+a_3+a_5+\dots+a_{19}=15 \\
 & \therefore a_2+a_4+a_6+\dots+a_{20}=-2
 \end{aligned}$$

$$\begin{array}{lcl}
 3. \quad a_3 - a_1 = 3 & a_7 = 9 + a_1 & 13 \quad 18 \quad 23 \quad 28 \quad 33 \quad 38 \quad 43 \\
 a_3 = 3 + a_1 & a_9 = 12 + a_1 & 15 \quad 21 \quad 25 \quad 30 \quad 35 \quad 40 \\
 a_5 - a_3 = 3 & a_{11} = 15 + a_1 & 17 \quad 24 \quad 27 \quad 34 \quad 37 \quad 44 \\
 a_5 = 6 + a_1 & & 19 \quad 29 \quad 29 \quad 42 \quad 39 \quad 51 \\
 & & 21 \quad 30 \quad 31 \quad 45
 \end{array}$$

$$\begin{aligned}
 &= 20(a_1+a_2) + (37(1+2+3+\dots+19) + 3(1+\dots+19)) \\
 &= 200 + 3 \left(\frac{18 \cdot 19}{2} \right) + 3 \left(\frac{19 \cdot 20}{2} \right) \\
 &= 200 + 510 + 570
 \end{aligned}$$

$$27(19) = \frac{243}{27} = 513$$

$$4. \quad \frac{11 \overbrace{111}^{109}}{11 \times 11 \times 10} = \frac{11^{109}}{10} \quad 11^{109} \pmod{10} = 1$$

$$f(x) = 3$$

$$6. \quad (f \circ g)'(x) = f'(g(x)) \cdot g'(x) = 3x^2 + 1$$

$$g'(x) = x^2 + \frac{1}{3}$$

$$g(x) = \frac{x^3}{3} + \frac{x}{3} = \frac{x^3}{12} + \frac{x^2}{5}$$

$$7. \quad 1 < -\frac{3}{7}x < 7$$

$$\frac{1}{3} < x < 7\frac{3}{7}$$

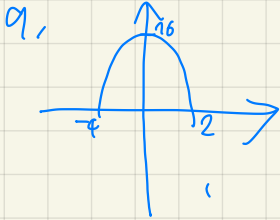
2, 3, 4, 5, 6, 7

$$8. \quad 75\% A + 87.5\% B = 120$$

$$3A + 3.5B = 480$$

$$A + \frac{3.5}{3}B = 160$$

$$\frac{3.5}{3}B = 160 - A$$



$$12. \quad 800 \times \frac{140}{100} = 1120$$

$$\frac{50}{100}x = 1120$$

$$15. \quad \frac{65 + 60}{2} = 62.5$$

$$14. \quad \{ \{ \dots \} \} \times \{ \dots \} \quad n = 13$$

$$= 1 \times 13 = 13$$

$$15. \quad \frac{\begin{pmatrix} 8 \\ 1 \end{pmatrix} \begin{pmatrix} 7 \\ 1 \end{pmatrix}}{\begin{pmatrix} 21 \\ 2 \end{pmatrix}} = \frac{2}{8 \times 7} \times \frac{21 \times 20 \times 5}{3}$$

16. 6, 16, 26, 36, 46, 56, 66, 76, 86, 96

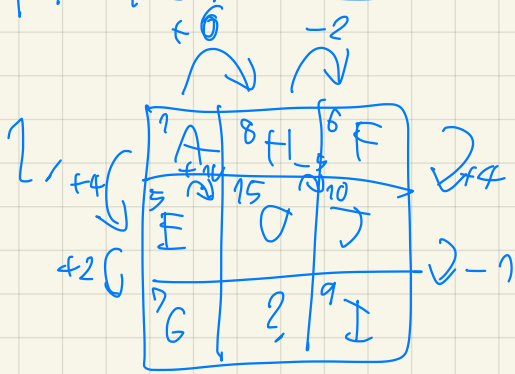
$$17. \quad 441 + 42 + 3$$

$$63 \times 7 + 14 \times 3 + 3$$

$$f(x+y+z) = 24x$$

$$y+z = 3x$$

PART 2

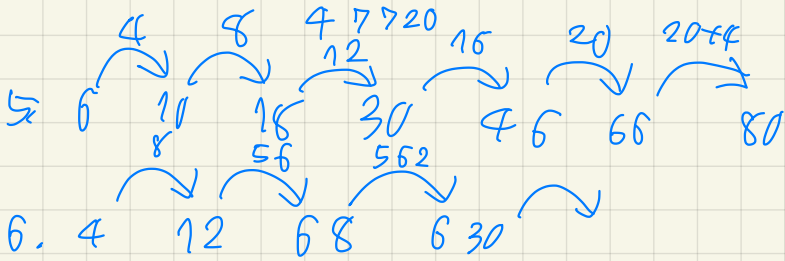


18, 21, 69
 L X S y M
 S y M
 M L X S

3, 65-65-77-89-101

29, A E G B D F C

4, $49,92 \times 2 = \frac{95,44}{100} \times 50000$



7, $9 \xrightarrow{\times 2} 18 \xrightarrow{-4} 14 \xrightarrow{\times 2} 28 \xrightarrow{-4} 24 \xrightarrow{\times 2} 48 \xrightarrow{-4} 44$

9, $+4^{+1} + 5^{+3} + 8^{+9} + 17^{+27} + 44$

13, $\frac{1}{2} (12)(120+60) = \frac{1080}{2}$

14, $\frac{640}{2^n} = 5$
 $2^n = 128$
 $n = 7$

