

$$S_1 = \frac{a_1(r^n - 1)}{r - 1}$$

$$\frac{2(2^n - 1)}{r - 1} = 510$$

$$2^n - 1 = 255$$

$$13 = \frac{a_1(r^n - 1)}{r - 1}$$

$$2^n = 256$$

$$n = 8$$

$$30 = \frac{a_1(r^{2n} - 1)}{r^2 - 1} \quad \textcircled{1}$$

$$-2 = a_2 + a_4 + \dots + a_{20} = \frac{a_2(r^{2n} - 1)}{r^2 - 1} \quad \textcircled{2}$$

$$\frac{a_2(r^{2n} - 1)}{r^2 - 1} \cdot \frac{r^2 - 1}{a_1(r^{2n} - 1)} = \frac{a_2}{a_1} = \frac{-2}{30} = -\frac{1}{15} = r$$

$$\textcircled{3} \quad a_1 + a_2 = 10$$

$$10 \nearrow 16$$

$$a_{n+2} = a_n + 3$$

$$40 \rightarrow 20$$

$$a_{n+1} = a_{n-1} + 3$$

$$S_{20} = 10$$

$$\therefore a_{n+1} + a_{n+2} = a_n + a_{n-1} + 6$$

$$a_n = 10 + (20-1) \cdot 6$$

$$= 10 + 19 \cdot 6 = 124$$

$$S_{20} = \left(\frac{10 + 124}{2} \right) \cdot 20 = 1340$$

$$11 \equiv 11 \pmod{1210}$$

$$11 \cdot 11 \cdot (11-1)$$

$$11^{11} = 1210 \cdot q + r$$

$$11^{11} = 11 \cdot 11 \cdot (10-1)q + r$$

$$11 \equiv 11 \pmod{1210}$$

$$|133|$$

$$|1210|$$

$$|121|$$

$$11^3 \equiv 1331 \pmod{1210}$$

$$11^2 \equiv 121 \pmod{1210}$$

$$11^3 \equiv 121 \pmod{1210}$$

$$11^4 \equiv$$

$$\int_0^1 \left(\frac{1}{3}x^3 + \frac{1}{2}x + 1 \right) dx$$

$$f(x) = 3x + 1 \rightarrow f'(x) = 3$$

$$= \left[\frac{1}{12}x^4 + \frac{1}{6}x^2 + x \right]_0^1$$

$$(f \circ g)'(x) = 3x^2 + 1 = f'(g(x)) \cdot g'(x)$$

$$= \frac{1}{12} + \frac{1}{6} + 1 - 0 = \frac{1+2+12}{12} = \frac{3}{4}$$

$$3x^2 + 1 = 3 \cdot g'(x)$$

$$g'(x) = x^2 + \frac{1}{3} \rightarrow \int g'(x) dx = \frac{1}{3}x^3 + \frac{1}{3}x + C = g(x) \quad \textcircled{4}$$

$$g(0) = 1$$

$$\frac{1}{3}x^3 + \frac{1}{3}x + 1$$

$$6 \xrightarrow{4} 10 \xrightarrow{8} 18 \xrightarrow{12} 30 \xrightarrow{16} 46 \xrightarrow{20} 66 \xrightarrow{24}$$

$$4 \xrightarrow{3} 12 \xrightarrow{\frac{17}{3}} 68 \xrightarrow{\frac{315}{39}} 630$$

$$12(5) + 4(2)$$

$$68(5) + 12(2)$$

$$1 \xrightarrow{3} 3 \xrightarrow{9} 27 \xrightarrow{81} 243$$

$$10 \xrightarrow{14} 19 \xrightarrow{27} 99 \xrightarrow{81} 827$$

$$\overbrace{5 \geq 4 \geq 3}$$

$$12(\frac{1}{2})$$

$$4 \xrightarrow{8} 12 \xrightarrow{54} 68 \xrightarrow{562} 630$$